

S.B. Roll No.....

APPLIED MATHEMATICS-II
2nd Exam/Common/0553/Jan'2022
(FOR 2018 BATCH ONWARDS)

Duration: 1.15Hrs.

M.Marks:25

SECTION-A

Q1. Attempt any three questions.

3x5=15

- Evaluate $\lim_{x \rightarrow 1} \frac{\sqrt{3+x} - \sqrt{5-x}}{x^2 - 1}$
- Find the equation of the normal to the curve $y = x^4 - 6x^3 + 13x^2 - 10x + 5$ at $(1, 3)$
- If $x = a(\theta + \sin \theta)$, $y = a(1 - \cos \theta)$, find $\frac{d^2y}{dx^2}$.
- Evaluate $\int \frac{dx}{x^2 - 4x + 8}$.
- Evaluate $\int x^2 \cot^{-1} x \, dx$
- Evaluate $\int_0^{\frac{\pi}{2}} \sin^5 x \cos^7 x \, dx$
- If $x^y = e^{x-y}$, prove that $\frac{dy}{dx} = \frac{\log x}{(1+\log x)^2}$.

SECTION-B

Q2. Attempt any one question.

1x10=10

- Find the maximum or minimum value of function $2x^3 - 15x^2 + 36x + 10$.

b) Evaluate $\int \frac{1}{x(x^4+1)} \, dx$

- c) Evaluate $\int_0^6 y \, dx$ by Simpson's rule given

x	0	1	2	3	4	5	6
y	0.146	0.161	0.176	0.190	0.204	0.217	0.230

- d) Solve the following LPP graphically:

Maximise and minimise $z = 5x + 10y$

subject to the constraints

$$x + 2y \leq 120,$$

$$x + y \geq 60,$$

$$x - 2y \geq 0,$$

$$x, y \geq 0.$$